

Кинематические инварианты

В некоторый момент времени известны скорости трех точек тела, движущегося в пространстве. Заданы координаты этих точек. Найти кинематические инварианты движения.

Задача К-29.1.

$$A = (0, 0, 0), B = (2, 0, 1), C = (1, 1, 1), \\ \vec{v}_A = (-1, 8, -4), \\ \vec{v}_B = (-9, -12, 12), \\ \vec{v}_C = (-1, -4, 8).$$

Задача К-29.3.

$$A = (1, 0, 2), B = (2, 1, 1), C = (1, 2, 1), \\ \vec{v}_A = (1, -2, -5), \\ \vec{v}_B = (5, -9, -8), \\ \vec{v}_C = (13, -1, -3).$$

Задача К-29.5.

$$A = (0, 2, 1), B = (2, 2, 2), C = (0, 0, -1), \\ \vec{v}_A = (-6, -4, 3), \\ \vec{v}_B = (-12, 16, 15), \\ \vec{v}_C = (20, -16, 15).$$

Задача К-29.7.

$$A = (0, 1, 1), B = (1, 1, 1), C = (1, -1, 1), \\ \vec{v}_A = (-4, 8, 4), \\ \vec{v}_B = (-4, -6, 9), \\ \vec{v}_C = (-32, -6, 13).$$

Задача К-29.9.

$$A = (1, 1, 1), B = (0, 1, 0), C = (2, 0, 0), \\ \vec{v}_A = (2, -8, -3), \\ \vec{v}_B = (-4, -9, 3), \\ \vec{v}_C = (3, 5, -15).$$

Задача К-29.11.

$$A = (0, 2, 0), B = (0, 0, 2), C = (-1, 2, 2), \\ \vec{v}_A = (-7, -2, -5), \\ \vec{v}_B = (-7, 6, 3), \\ \vec{v}_C = (-23, -2, -13).$$

Задача К-29.13.

$$A = (0, 1, 0), B = (0, 2, 1), C = (-1, 2, 0), \\ \vec{v}_A = (-1, -8, -2), \\ \vec{v}_B = (-17, -4, -6), \\ \vec{v}_C = (-9, -16, -14).$$

Задача К-29.2.

$$A = (1, 0, 1), B = (-1, 0, 1), C = (2, 2, 0), \\ \vec{v}_A = (5, -7, -1), \\ \vec{v}_B = (5, 21, 9), \\ \vec{v}_C = (28, -23, -10).$$

Задача К-29.4.

$$A = (1, 2, 2), B = (0, 0, -1), C = (-1, 1, 0), \\ \vec{v}_A = (2, -8, -1), \\ \vec{v}_B = (34, -33, 5), \\ \vec{v}_C = (21, -34, -7).$$

Задача К-29.6.

$$A = (1, 1, 1), B = (-1, 0, 3), C = (0, 1, 1), \\ \vec{v}_A = (4, -4, 5), \\ \vec{v}_B = (19, -10, 17), \\ \vec{v}_C = (4, -11, 9).$$

Задача К-29.8.

$$A = (0, 2, 1), B = (2, 0, 1), C = (1, 0, 1), \\ \vec{v}_A = (-1, 5, 4), \\ \vec{v}_B = (17, 23, 12), \\ \vec{v}_C = (17, 14, 6).$$

Задача К-29.10.

$$A = (1, 2, 1), B = (1, 0, 2), C = (1, 0, 1), \\ \vec{v}_A = (2, -8, -3), \\ \vec{v}_B = (22, -2, 9), \\ \vec{v}_C = (16, -8, 9).$$

Задача К-29.12.

$$A = (2, 2, 0), B = (0, 1, 2), C = (-1, 0, 1), \\ \vec{v}_A = (-6, 7, -5), \\ \vec{v}_B = (25, -11, 17), \\ \vec{v}_C = (26, -24, 29).$$

Задача К-29.14.

$$A = (1, 2, 2), B = (2, 1, 0), C = (1, 2, -1), \\ \vec{v}_A = (4, 8, 5), \\ \vec{v}_B = (28, 26, 8), \\ \vec{v}_C = (19, 14, 5).$$

Задача K-29.15.

$A = (0, 1, 0)$, $B = (2, 3, 2)$, $C = (1, 1, 1)$,
 $\vec{v}_A = (-4, -3, 2)$,
 $\vec{v}_B = (-4, -9, 8)$,
 $\vec{v}_C = (-10, -6, 8)$.

Задача K-29.17.

$A = (2, 1, 1)$, $B = (-1, 1, 0)$, $C = (0, 1, 0)$,
 $\vec{v}_A = (-1, -5, 3)$,
 $\vec{v}_B = (-7, -34, 21)$,
 $\vec{v}_C = (-7, -25, 15)$.

Задача K-29.19.

$A = (1, 1, 2)$, $B = (-1, 2, 1)$, $C = (0, 1, 1)$,
 $\vec{v}_A = (4, -5, -5)$,
 $\vec{v}_B = (4, 7, 7)$,
 $\vec{v}_C = (-4, -1, 3)$.

Задача K-29.21.

$A = (1, 0, 2)$, $B = (0, 0, 1)$, $C = (1, 1, 1)$,
 $\vec{v}_A = (5, 6, 3)$,
 $\vec{v}_B = (-7, 17, 15)$,
 $\vec{v}_C = (5, 5, 2)$.

Задача K-29.23.

$A = (1, 0, 1)$, $B = (2, 1, 1)$, $C = (2, 1, 0)$,
 $\vec{v}_A = (4, -6, 4)$,
 $\vec{v}_B = (11, -13, 4)$,
 $\vec{v}_C = (5, -7, 4)$.

Задача K-29.25.

$A = (0, 1, 1)$, $B = (2, 1, 2)$, $C = (0, 1, 0)$,
 $\vec{v}_A = (-4, -7, 1)$,
 $\vec{v}_B = (-16, 18, 25)$,
 $\vec{v}_C = (8, -8, 1)$.

Задача K-29.27.

$A = (1, 0, 1)$, $B = (0, -1, -1)$, $C = (2, 0, 0)$,
 $\vec{v}_A = (5, -4, -3)$,
 $\vec{v}_B = (13, -4, -7)$,
 $\vec{v}_C = (13, -16, 5)$.

Задача K-29.16.

$A = (1, 1, 2)$, $B = (1, 2, 2)$, $C = (0, 1, 2)$,
 $\vec{v}_A = (2, 2, -2)$,
 $\vec{v}_B = (8, 2, -4)$,
 $\vec{v}_C = (2, 8, -5)$.

Задача K-29.18.

$A = (1, 1, 2)$, $B = (2, 0, 1)$, $C = (0, 0, 1)$,
 $\vec{v}_A = (3, -6, -4)$,
 $\vec{v}_B = (3, 6, -16)$,
 $\vec{v}_C = (3, -10, 0)$.

Задача K-29.20.

$A = (0, 0, 1)$, $B = (2, 2, 1)$, $C = (2, 2, 0)$,
 $\vec{v}_A = (-5, 7, 1)$,
 $\vec{v}_B = (23, -21, 15)$,
 $\vec{v}_C = (28, -19, 15)$.

Задача K-29.22.

$A = (1, 0, 1)$, $B = (-1, 0, 0)$, $C = (1, 1, 1)$,
 $\vec{v}_A = (8, -1, 4)$,
 $\vec{v}_B = (0, 11, 20)$,
 $\vec{v}_C = (16, -1, 0)$.

Задача K-29.24.

$A = (2, 0, 0)$, $B = (2, -1, -1)$, $C = (1, -1, 0)$,
 $\vec{v}_A = (-2, -6, -4)$,
 $\vec{v}_B = (-13, -2, -8)$,
 $\vec{v}_C = (-9, 1, -4)$.

Задача K-29.26.

$A = (1, 2, 1)$, $B = (1, 0, -1)$, $C = (1, 6, 1)$,
 $\vec{v}_A = (8, 1, -2)$,
 $\vec{v}_B = (40, -7, 6)$,
 $\vec{v}_C = (-24, 1, -18)$.

Задача K-29.28.

$A = (0, 1, 0)$, $B = (3, 1, 1)$, $C = (1, 0, 1)$,
 $\vec{v}_A = (-5, -7, 2)$,
 $\vec{v}_B = (-10, 33, 17)$,
 $\vec{v}_C = (4, 5, 5)$.

K-29 Ответы.**Кинематические инварианты**

30.10.2013

| № | ω_x | ω_y | ω_z | ω | $\vec{\omega} \cdot \vec{v}_A$ |
|----|------------|------------|------------|----------|--------------------------------|
| 1 | 4 | -8 | -8 | 12 | -36 |
| 2 | -2 | 5 | -14 | 15 | -31 |
| 3 | 1 | 4 | -8 | 9 | 33 |
| 4 | -6 | -6 | 7 | 11 | 29 |
| 5 | -6 | -6 | 7 | 11 | 81 |
| 6 | -4 | 4 | 7 | 9 | 3 |
| 7 | -2 | -5 | -14 | 15 | -88 |
| 8 | 2 | -6 | 9 | 11 | 4 |
| 9 | 6 | 6 | 7 | 11 | -57 |
| 10 | -6 | 6 | 7 | 11 | -81 |
| 11 | -4 | -8 | 8 | 12 | 4 |
| 12 | -2 | 10 | 11 | 15 | 27 |
| 13 | -4 | -8 | 8 | 12 | 52 |
| 14 | 2 | -5 | 14 | 15 | 38 |
| 15 | -3 | -6 | -6 | 9 | 18 |
| 16 | -2 | -3 | -6 | 7 | 2 |
| 17 | -2 | 6 | 9 | 11 | -1 |
| 18 | 4 | 8 | 8 | 12 | -68 |
| 19 | -4 | 8 | -8 | 12 | -16 |
| 20 | 2 | -5 | -14 | 15 | -59 |
| 21 | -1 | 12 | -12 | 17 | 31 |
| 22 | -4 | 8 | -8 | 12 | -72 |
| 23 | 6 | 6 | -7 | 11 | -40 |
| 24 | 4 | 4 | -7 | 9 | -4 |
| 25 | -1 | -12 | 12 | 17 | 100 |
| 26 | -4 | -8 | 8 | 12 | -56 |
| 27 | -4 | -8 | -8 | 12 | 36 |
| 28 | 2 | -5 | 14 | 15 | 53 |

K-29 файл o29k6A