

Кинематические инварианты

В некоторый момент времени известны скорости трех точек тела, движущегося в пространстве. Заданы координаты этих точек. Найти кинематические инварианты движения.

Задача К-29.1.

$$A = (2, 1, 0), B = (-1, 2, 0), C = (0, 1, 0), \\ \vec{v}_A = (-4, -5, -1), \\ \vec{v}_B = (4, 19, 19), \\ \vec{v}_C = (-4, 11, 15).$$

Задача К-29.2.

$$A = (0, 2, 0), B = (3, 1, 2), C = (0, 0, 0), \\ \vec{v}_A = (-8, -8, -2), \\ \vec{v}_B = (-14, 24, 23), \\ \vec{v}_C = (24, -8, -18).$$

Задача К-29.3.

$$A = (0, 2, 0), B = (1, 1, 3), C = (0, 0, 2), \\ \vec{v}_A = (-1, 4, 3), \\ \vec{v}_B = (-9, 14, 9), \\ \vec{v}_C = (-1, 8, 7).$$

Задача К-29.4.

$$A = (0, 1, 0), B = (2, 2, 1), C = (1, 0, 1), \\ \vec{v}_A = (-1, 2, -4), \\ \vec{v}_B = (3, -15, 5), \\ \vec{v}_C = (-13, -7, -1).$$

Задача К-29.5.

$$A = (1, 1, 2), B = (2, 1, 1), C = (1, 1, 1), \\ \vec{v}_A = (4, -7, -2), \\ \vec{v}_B = (-8, -18, -14), \\ \vec{v}_C = (-8, -6, -2).$$

Задача К-29.6.

$$A = (2, 2, 0), B = (1, 1, 2), C = (0, 1, 0), \\ \vec{v}_A = (-3, -1, 4), \\ \vec{v}_B = (9, -3, 9), \\ \vec{v}_C = (3, -13, 12).$$

Задача К-29.7.

$$A = (0, 1, 0), B = (2, 1, 1), C = (0, 5, 0), \\ \vec{v}_A = (-8, -8, -3), \\ \vec{v}_B = (-19, -32, 19), \\ \vec{v}_C = (56, -8, -35).$$

Задача К-29.8.

$$A = (0, 1, 0), B = (2, 1, 1), C = (2, 3, 0), \\ \vec{v}_A = (-5, 3, 5), \\ \vec{v}_B = (-9, -15, 13), \\ \vec{v}_C = (9, -11, 21).$$

Задача К-29.9.

$$A = (1, 2, 2), B = (3, -1, -1), C = (0, 0, 1), \\ \vec{v}_A = (2, -2, -1), \\ \vec{v}_B = (29, 16, -1), \\ \vec{v}_C = (17, -6, -8).$$

Задача К-29.10.

$$A = (1, 0, 1), B = (0, -1, 1), C = (2, 0, 1), \\ \vec{v}_A = (4, 8, -3), \\ \vec{v}_B = (-10, 22, 4), \\ \vec{v}_C = (4, -6, -8).$$

Задача К-29.11.

$$A = (2, 2, 1), B = (0, 1, 0), C = (0, 3, -1), \\ \vec{v}_A = (-2, 6, 3), \\ \vec{v}_B = (1, -12, 15), \\ \vec{v}_C = (-17, -16, 7).$$

Задача К-29.12.

$$A = (1, 1, 1), B = (1, 1, 2), C = (0, -1, 0), \\ \vec{v}_A = (2, 8, 5), \\ \vec{v}_B = (-4, 14, 5), \\ \vec{v}_C = (22, -5, 11).$$

Задача К-29.13.

$$A = (1, 2, 1), B = (0, 0, 0), C = (2, 2, -1), \\ \vec{v}_A = (1, -4, -1), \\ \vec{v}_B = (5, -6, -1), \\ \vec{v}_C = (-7, 4, -5).$$

Задача К-29.14.

$$A = (1, 1, 1), B = (0, 2, 1), C = (2, 3, 0), \\ \vec{v}_A = (3, -7, 2), \\ \vec{v}_B = (10, 0, 14), \\ \vec{v}_C = (11, -8, 8).$$

Задача K-29.15.

$A = (0, 2, 1)$, $B = (2, 2, 2)$, $C = (2, 2, 0)$,
 $\vec{v}_A = (-7, 3, -3)$,
 $\vec{v}_B = (-13, 11, 9)$,
 $\vec{v}_C = (-1, 23, 9)$.

Задача K-29.17.

$A = (0, 1, 0)$, $B = (1, 3, 0)$, $C = (-1, 1, 0)$,
 $\vec{v}_A = (-2, 1, -5)$,
 $\vec{v}_B = (-18, 9, -3)$,
 $\vec{v}_C = (-2, -7, -9)$.

Задача K-29.19.

$A = (1, 1, 1)$, $B = (1, 1, 2)$, $C = (0, 0, 1)$,
 $\vec{v}_A = (6, -4, 1)$,
 $\vec{v}_B = (12, 2, 1)$,
 $\vec{v}_C = (13, -11, 13)$.

Задача K-29.21.

$A = (1, 0, 2)$, $B = (2, -1, 0)$, $C = (1, 1, 0)$,
 $\vec{v}_A = (1, 8, -4)$,
 $\vec{v}_B = (9, 8, 0)$,
 $\vec{v}_C = (25, 16, 0)$.

Задача K-29.23.

$A = (0, 1, 1)$, $B = (1, 1, 0)$, $C = (1, 1, -1)$,
 $\vec{v}_A = (-6, 4, 4)$,
 $\vec{v}_B = (0, -9, 10)$,
 $\vec{v}_C = (6, -15, 10)$.

Задача K-29.25.

$A = (1, 1, 2)$, $B = (2, 1, 0)$, $C = (1, 2, 0)$,
 $\vec{v}_A = (4, 7, 4)$,
 $\vec{v}_B = (28, 21, 16)$,
 $\vec{v}_C = (16, 9, 5)$.

Задача K-29.27.

$A = (0, 1, 1)$, $B = (0, 1, 2)$, $C = (2, 0, 1)$,
 $\vec{v}_A = (-2, -4, -1)$,
 $\vec{v}_B = (-8, -2, -1)$,
 $\vec{v}_C = (-11, -22, 13)$.

Задача K-29.16.

$A = (1, 2, 2)$, $B = (-1, 1, 1)$, $C = (-1, 3, 1)$,
 $\vec{v}_A = (3, -5, -2)$,
 $\vec{v}_B = (6, -23, 10)$,
 $\vec{v}_C = (-8, -23, 2)$.

Задача K-29.18.

$A = (0, 0, 0)$, $B = (1, -1, 0)$, $C = (0, -1, 2)$,
 $\vec{v}_A = (-7, 8, -5)$,
 $\vec{v}_B = (-19, -4, 12)$,
 $\vec{v}_C = (-37, 24, 3)$.

Задача K-29.20.

$A = (1, 2, 1)$, $B = (3, 0, 2)$, $C = (1, 1, 1)$,
 $\vec{v}_A = (8, -3, 1)$,
 $\vec{v}_B = (20, 20, 23)$,
 $\vec{v}_C = (20, -3, 0)$.

Задача K-29.22.

$A = (2, 2, 1)$, $B = (0, 0, 1)$, $C = (1, 1, 0)$,
 $\vec{v}_A = (-7, 6, -1)$,
 $\vec{v}_B = (15, -16, 23)$,
 $\vec{v}_C = (-6, -7, 11)$.

Задача K-29.24.

$A = (0, 2, 1)$, $B = (3, 0, 0)$, $C = (1, 0, 1)$,
 $\vec{v}_A = (-3, -1, 2)$,
 $\vec{v}_B = (12, 19, 7)$,
 $\vec{v}_C = (9, 5, 1)$.

Задача K-29.26.

$A = (0, 2, 1)$, $B = (2, 2, 1)$, $C = (2, 1, -1)$,
 $\vec{v}_A = (-6, 5, -1)$,
 $\vec{v}_B = (-6, 29, 23)$,
 $\vec{v}_C = (30, 31, 22)$.

Задача K-29.28.

$A = (1, 2, 1)$, $B = (1, 0, 2)$, $C = (0, 0, 0)$,
 $\vec{v}_A = (6, -2, 2)$,
 $\vec{v}_B = (24, 2, 10)$,
 $\vec{v}_C = (16, -13, 14)$.

K-29 Ответы.**Кинематические инварианты**

30.10.2013

№	ω_x	ω_y	ω_z	ω	$\vec{\omega} \cdot \vec{v}_A$
1	-4	8	-8	12	-16
2	8	-11	16	21	-8
3	-2	-4	4	6	-2
4	1	-4	-8	9	23
5	1	12	-12	17	-56
6	-2	3	6	7	27
7	-8	-11	-16	21	200
8	4	-4	-7	9	-67
9	2	-3	6	7	4
10	-2	5	-14	15	74
11	-4	4	7	9	53
12	-6	-6	7	11	-25
13	2	4	4	6	-18
14	6	6	-7	11	-38
15	6	-6	7	11	-81
16	-4	4	7	9	-46
17	-1	-4	8	9	-42
18	-8	-9	-12	17	44
19	-6	6	7	11	-53
20	1	-12	12	17	56
21	4	-8	-8	12	-28
22	-2	10	11	15	63
23	-6	-6	-7	11	-16
24	2	-3	6	7	9
25	1	-12	12	17	-32
26	1	-12	12	17	-78
27	-2	-6	-9	11	37
28	-4	4	7	9	-18

K-29 файл o29k5A